

## Chapter 3

### Question 3.7

The glycerol molecule ( $C_3H_8O_3$ ) is not electrically charged (see Figure D in Box 2.1). From Equation 3.3 it follows that the membrane permeability to glycerol can then be calculated by dividing the measured value of the glycerol flux ( $0.02 \text{ mmol m}^{-2} \text{ s}^{-1}$ ) by the concentration difference of glycerol across the membrane ( $10 \text{ mmol L}^{-1} - 0 \text{ mmol L}^{-1} = 10 \text{ mmol L}^{-1}$ ) which yields a value of  $2 \times 10^{-6} \text{ m s}^{-1}$  for membrane permeability to glycerol ( $0.02 \text{ mmol m}^{-2} \text{ s}^{-1} / 10 \text{ mmol L}^{-1} = 0.002 \text{ (mmol/mmol)} \times (\text{m}^{-2} \text{ L}) \text{ s}^{-1} = 0.002 \times 1 \times (\text{m}^{-2} \times 10^{-3} \text{ m}^3) \text{ s}^{-1} = 2 \times 10^{-6} \text{ m s}^{-1}$ ). **Since the glycerol molecule is not electrically charged, its rate of entry across the membrane does not depend on the electrical potential difference across the membrane.**

### Question 3.9

The equilibrium potential for  $\text{Na}^+$  is calculated using Equation 3.6:

$$V_{\text{right-left}}^{\text{ion}} = 2.3 \frac{RT}{zF} \log \frac{[\text{ion}_{\text{left}}]}{[\text{ion}_{\text{right}}]} \quad \text{Equation 3.6}$$

where  $R$  is the gas constant ( $8.31 \text{ J mol}^{-1} \text{ K}^{-1}$ ),  $T$  is the absolute temperature ( $273 + 7 \text{ K} = 280 \text{ K}$ ),  $z$  is the charge carried by the  $\text{Na}^+$  ion ( $+1$ ),  $F$  is the Faraday number representing the number of electrical charges carried by one mol of monovalent ions ( $96,485 \text{ C mol}^{-1}$ ),  $[\text{ion}_{\text{left}}]$  is the concentration of  $\text{Na}^+$  on the left side of the barrier ( $100 \text{ mmol L}^{-1}$ ) and  $[\text{ion}_{\text{right}}]$  is the concentration of  $\text{Na}^+$  on the right side of the barrier ( $50 \text{ mmol L}^{-1}$ ). Substituting the various parameters in Equation 3.6, it follows that:

$$\begin{aligned} V_{\text{right-left}}^{\text{Na}} &= 2.3 \times 8.31 \text{ J mol}^{-1} \text{ K}^{-1} \times 280 \text{ K} / 96,485 \text{ C mol}^{-1} \times \log (100 \text{ mmol L}^{-1} / 50 \text{ mmol L}^{-1}) \\ &= 0.0555 \text{ J C}^{-1} \times \log 2 \\ &= 0.0167 \text{ J C}^{-1} \\ &= \mathbf{16.7 \text{ mV}} \text{ because } 1 \text{ J C}^{-1} = 1 \text{ V} \text{ as explained in Box 3.1. This means that the sodium ion will be at equilibrium between the two compartments separated by the barrier, when the electrical potential on the right side of the barrier is 16.7 mV more positive than the electrical potential on the left side of the barrier.} \end{aligned}$$

Note that the equilibrium potential of an ion (sodium ion in this case) does not change when the concentration of the respective ion changes by the same factor on both sides of the barrier, because the equilibrium potential of an ion depends on the logarithm of the ratio between the concentrations of the respective ion on the two sides of the barrier. **Therefore, doubling the  $\text{Na}^+$  concentration on both sides of the barrier ( $200 \text{ mmol L}^{-1}$  from  $100 \text{ mmol L}^{-1}$  on the left and  $100 \text{ mmol L}^{-1}$  from  $50 \text{ mmol L}^{-1}$  on the right side of the barrier) does not change the value of the  $\log [\text{Na}^+_{\text{left}}] / [\text{Na}^+_{\text{right}}]$  which remains  $\log 2 = 0.301$ .**

### Question 3.10

The Goldman-Hodgkin-Katz equation (Equation 3.9) is reproduced below:

**Butler, Brown, Stephenson & Speakman, *Animal Physiology*  
Solutions to numerical exercises**

$$V_{\text{right-left}}^{\text{GHK}} = 2.3 \frac{RT}{F} \log \frac{P_{\text{K}}[\text{K}^+_{\text{left}}] + P_{\text{Na}}[\text{Na}^+_{\text{left}}] + P_{\text{Cl}}[\text{Cl}^-_{\text{right}}]}{P_{\text{K}}[\text{K}^+_{\text{right}}] + P_{\text{Na}}[\text{Na}^+_{\text{right}}] + P_{\text{Cl}}[\text{Cl}^-_{\text{left}}]} \quad \text{Equation 3.9}$$

The term  $2.3 RT/F$  for  $17^\circ\text{C}$  ( $T = 273 + 17 = 290 \text{ K}$ ) amounts to  $57.4 \text{ mV}$ :

$$\begin{aligned} & 2.3 \times 8.31 \text{ J mol}^{-1} \text{ K}^{-1} \times 290 \text{ K} / 96,485 \text{ C mol}^{-1} \\ &= 0.0574 \text{ J C}^{-1} \\ &= 0.0574 \text{ V} \\ &= 57.4 \text{ mV since } 1 \text{ J C}^{-1} = 1 \text{ V as explained in Box 3.1.} \end{aligned}$$

Using the values for  $\text{Na}^+$  and  $\text{Cl}^-$  permeabilities relative to  $\text{K}^+$  permeability and the ion concentrations in the text of Question 3.10, the numerator of the log fraction becomes:

$$\begin{aligned} & P_{\text{K}} \times 10 \text{ mmol L}^{-1} + P_{\text{Na}} \times 100 \text{ mmol L}^{-1} + P_{\text{Cl}} \times 110 \text{ mmol L}^{-1} \\ &= P_{\text{K}} \times 10 \text{ mmol L}^{-1} + 0.01 P_{\text{K}} \times 100 \text{ mmol L}^{-1} + 0.01 P_{\text{K}} \times 110 \text{ mmol L}^{-1} \\ &= 12.1 P_{\text{K}} \text{ mmol L}^{-1}. \end{aligned}$$

Similarly, for the conditions indicated in the text of Question 3.10, the denominator of the log fraction becomes:

$$\begin{aligned} & P_{\text{K}} \times 100 \text{ mmol L}^{-1} + 0.01 P_{\text{K}} \times 10 \text{ mmol L}^{-1} + 0.01 P_{\text{K}} \times 110 \text{ mmol L}^{-1} \\ &= 101.2 P_{\text{K}} \text{ mmol L}^{-1}. \end{aligned}$$

Therefore, the value of log term in Equation 3.9 is:  $\log (12.1 P_{\text{K}} \text{ mmol L}^{-1} / 101.2 P_{\text{K}} \text{ mmol L}^{-1}) = \log 0.1196 = -0.922$ .

Consequently,  $V_{\text{right-left}}^{\text{GHK}} = 57.4 \text{ mV} \times (-0.922) = \mathbf{-52.95 \text{ mV}}$